

ASME BPVC VIII-1 2021

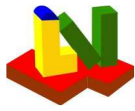
Example E4.4.7 - E4.4.8 PTB-4-2013

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Layout

Input values:	1.234	or	1.234
Calculated values:	1.234	or	1.234
Critical values:	1.234	or	1.234
Estimated values:	1.234	or	1.234



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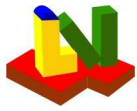
Example E4.4.7 - E4.4.8 PTB-4-2013

Summary

Strength Calculation Software	Program System ATLAS	Version	8.33.8						
Developed by Lauterbach Verfahrenstechnik GmbH									
Certified per DIN EN ISO 9001:2015				Certificate Number 01 100 044763					
				LV Soft			ASME		Diff [%]
Example E4.4.7 - Conical transition Without a knuckle (large End)									
		Required area ArL	1008.88 mm ²	1.56 in ²			1.56 in ²		0.10%
		Required area AeL	13064.03 mm ²	20.25 in ²			32.14 in ²		37.00%
Large End/Line-of-support		Required moment of inertia Is	33871336.00 mm ⁴	81.38 in ⁴			81.85 in ⁴		0.57%
		Required moment of inertia I's	43504464.00 mm ⁵	104.52 in ⁵			105.12 in ⁵		0.57%
Example E4.4.7 - Conical transition Without a knuckle (Small End)									
		Required area ArS	715.96 mm ²	1.11 in ²			1.11 in ²		0.08%
		Required area AeS	8001.92 mm ²	12.40 in ²			10.11 in ²		22.65%
Small End/Line-of-support		Required moment of inertia Is	6975754.00 mm ⁴	16.76 in ⁴			16.76 in ⁴		0.02%
		Required moment of inertia I's	8959684.00 mm ⁴	21.53 in ⁴			21.53 in ⁴		0.02%
Example E4.4.8 - Conical transition With a knuckle									
Large End/Line-of-support		Required moment of inertia Is	5850143.00 mm ⁴	14.06 in ⁴			13.82 in ⁴		1.70%
		Required moment of inertia I's	7513945.00 mm ⁴	18.05 in ⁴			17.75 in ⁴		1.70%

Equations for Aes und Ael in Appendices 1-5 and 1-8 have been changed in Edition 2021!

Results have to be adapted accordingly. Basis is PTB 4-2013!



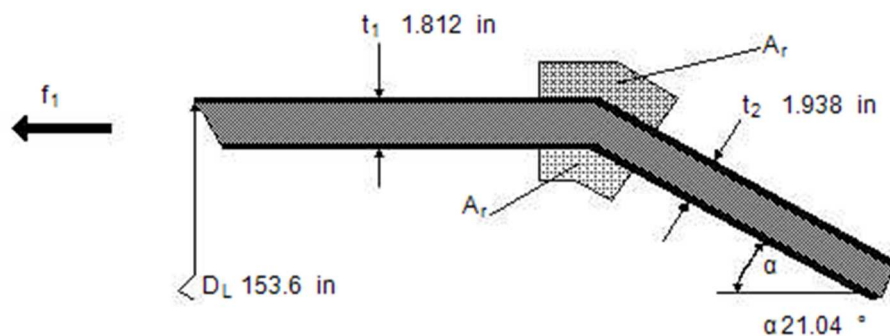
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Example E4.4.7 - E4.4.8 PTB-4-2013

E4.4.7 Large End - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2021

Area at the wide end of a cone-cylinder-juncture without knuckle acc. App.1-8

Type of stiffener No stiffener

External design pressure	p_D	14.7 psi
Hydrostatic head	D_p	0 psi
Calculation pressure	p_0	14.7 psi
Calculation temperature	T_0	300 °F
Axial additional load as line load (positive for tension) e.g. wind load, dead weight, traffic load, etc. but no loads resulting from internal / external pressure	f_1	497.1 lbf/in



Cylinder

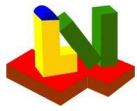
Final wall thickness	t_1	1.812 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Final thickness without allowances	t_s	1.687 in
Outside diameter	D_L	153.6 in
Tip radius ($=D_L/2$)	R_L	76.8 in
Required thickness without allowances (UG-28)	t_{1r}	0.9549 in
Required thickness with allowances (UG-28)	t_{1r+}	1.08 in
Joint efficiency factor	E_1	1
Material K02700-SA-516-70-Class:-Size:		
Allowable stress	S_s	20015 psi
Modulus of elasticity	E_s	2.9e+7 psi

Cone

Final wall thickness	t_2	1.938 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Final thickness without allowances	t_c	1.813 in
Half apex angle ($\leq 60^\circ$)	α	21.04 °
Required thickness without allowances (UG-33)	t_{2r}	0.3639 in
Required thickness with allowances (UG-33)	t_{2r+}	0.4889 in
Joint efficiency factor	E_2	1
Material K02700-SA-516-70-Class:-Size:		
Allowable stress	S_c	20015 psi
Modulus of elasticity	E_c	2.9e+7 psi

Stiffening ring

Material K02700-SA-516-70-Class:-Size:		
Actual cross section of the stiffener	A_r	34 in ²
Allowable stress	S_r	20015 psi
Modulus of elasticity	E_r	2.9e+7 psi



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Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Factor (≥ 1)
 Ratio
 Angle
 Effective load
 Cross sectional area
 Effective area

k **1**
 $P_0/S_s E_1$ **7.344e-4**
 D_{el} **2.818** °
 Q_L **1062** lbf/in
 A_{rL} **1.564** in²
 A_{eL} **20.25** in²

 A_{req} **0** in²

Required cross section of reinforcement

Remark **Stiffening required acc. App. 1-8 (b)**

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

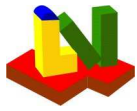
$$Q_L = P_0 \cdot \frac{R_L}{2} + f_1 = 1.014 \text{ bar} \cdot \frac{1951 \text{ mm}}{2} + 87.06 \text{ N/mm} = 185.9 \text{ N/mm}$$

$$A_{rL} = \frac{k \cdot Q_L \cdot R_L \cdot \tan(\alpha)}{S_s \cdot E_1} \cdot \left(1 - \frac{P_0 \cdot R_L - Q_L}{4 \cdot Q_L} \cdot \frac{D_{el}}{\alpha} \right) = \quad (1)$$

$$\frac{1 \cdot 185.9 \text{ N/mm} \cdot 1951 \text{ mm} \cdot 0.3846}{138 \text{ N/mm}^2 \cdot 1} \cdot \left(1 - \frac{1.014 \text{ bar} \cdot 1951 \text{ mm} - 185.9 \text{ N/mm}}{4 \cdot 185.9 \text{ N/mm}} \cdot \frac{2.818^\circ}{21.04^\circ} \right) = 1009 \text{ mm}^2$$

$$A_{eL} = 0.55 \cdot \sqrt{(D_L \cdot t_s)} \cdot \left(\frac{t_s + t_c}{\cos(\alpha)} \right) = \quad (2)$$

$$0.55 \cdot \sqrt{(3902 \text{ mm} \cdot 42.86 \text{ mm})} \cdot \left(\frac{42.86 \text{ mm} + 46.04 \text{ mm}}{0.9333} \right) = 13064 \text{ mm}^2$$



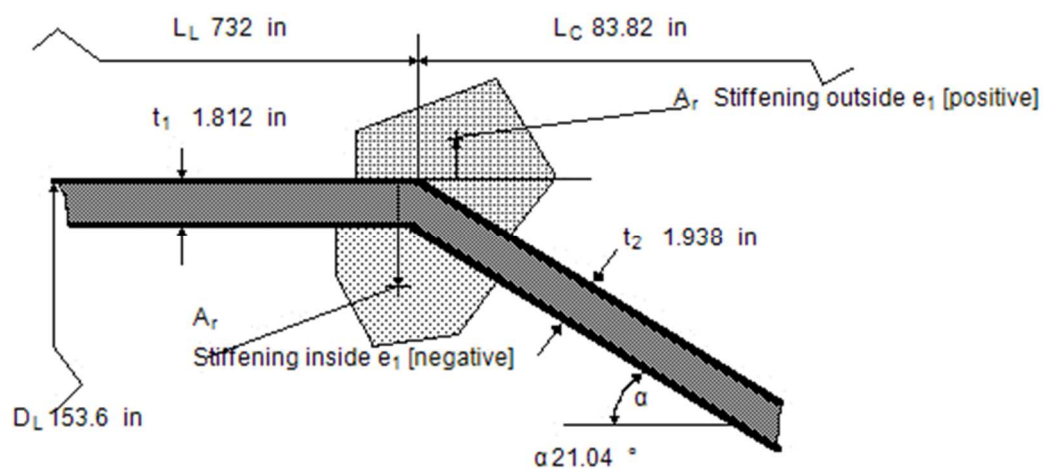
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Example E4.4.7 - E4.4.8 PTB-4-2013

E4.4.7 Large End/Line-of-support - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2021

Moment of inertia at the wide end of a cone-cylinder-juncture under external pressure acc. App. 1-8

(Line-of-support)

External design pressure	p_D	14.7 psi
Hydrostatic head	D_p	0 psi
Calculation pressure	p_0	14.7 psi
Calculation temperature	T_0	300 °F
Axial additional load as line load (positive for tension) e.g. wind load, dead weight, traffic load, etc. but no loads resulting from internal / external pressure	f_1	497.1 lbf/in



Cylinder

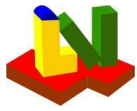
Design wall thickness	t_1	1.812 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Final thickness without allowances	t_s	1.687 in
Required thickness without allowances (UG-28)	t_{1r}	0.9549 in
Required thickness with allowances (UG-28)	t_{1r+}	1.08 in
Outside diameter	D_L	153.6 in
Tip radius ($=D_L/2$)	R_L	76.81 in
Buckling length	L_L	732 in

Cone

Design wall thickness	t_2	1.938 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Final thickness without allowances	t_c	1.813 in
Required thickness without allowances (UG-33)	t_{2r}	0.3639 in
Required thickness with allowances (UG-33)	t_{2r+}	0.4889 in
Half apex angle ($\leq 60^\circ$)	α	21.04 °
Buckling length	L_C	83.82 in

Stiffening ring

Material	K02700-SA-516-70-Class:-Size:	
Spec. Min. Yield	S_y	2.9e+7 psi
Applicable material chart	Fig	CS-2
Radial distance between the centroid of the stiffening ring and the outer surface of the cylinder	e_1	in
Cross sectional area	A_r	0 in ²
Moment of inertia	I_r	in ⁴



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Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Equivalent length	M	393.8 in
Effective load	F_L	5980 lbf/in
Reference area	A_{TL}	693.6 in ²
Factor	B	993.4 psi
Factor (see material chart)	A	6.96e-5
Required moment of inertia	I_s	81.38 in ⁴
Required moment of inertia	I'_s	104.5 in ⁴
Length of support	$0.55 \cdot \sqrt{(D \cdot t_s)}$	8.856 in
Available moment of inertia	I'	in ⁴

Remark

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\sin(\alpha) = \sin(\alpha) = \sin(21.04^\circ) = 0.359$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$R_s = R_L - L_C \cdot \sin(\alpha) = 1951 \text{ mm} - 2129 \text{ mm} \cdot 0.359 = 1172 \text{ mm}$$

$$M = \frac{-R_L \cdot \tan(\alpha)}{2} + \frac{L_L}{2} + \frac{RL^2 - RS^2}{3 \cdot R_L \cdot \tan(\alpha)} =$$

$$\frac{-1951 \text{ mm} \cdot 0.3846}{2} + \frac{18593 \text{ mm}}{2} + \frac{(1951 \text{ mm})^2 - (1172 \text{ mm})^2}{3 \cdot 1951 \text{ mm} \cdot 0.3846} = 10002 \text{ mm}$$

App. 1-8 b-3) Step 1

$$F_L = P_0 \cdot M + f_1 \cdot \tan(\alpha) =$$

$$1.014 \text{ bar} \cdot 10002 \text{ mm} + 87.06 \text{ N/mm} \cdot 0.3846 = 1047 \text{ N/mm}$$

App. 1-8 b-3) Step 1

$$A_{TL} = L_L \cdot \frac{t_s}{2} + L_C \cdot \frac{t_c}{2} + A_s =$$

$$18593 \text{ mm} \cdot \frac{42.86 \text{ mm}}{2} + 2129 \text{ mm} \cdot \frac{46.04 \text{ mm}}{2} + 0 \text{ mm}^2 = 447474 \text{ mm}^2$$

App. 1-8 a)

$$B = \frac{3}{4} \cdot \frac{F_L \cdot D_L}{A_{TL}} = \frac{3}{4} \cdot \frac{1047 \text{ N/mm} \cdot 3902 \text{ mm}}{447474 \text{ mm}^2} = 6.849 \text{ N/mm}^2$$

App. 1-8 b-3) Step 1

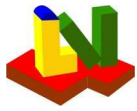
$$I_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{14} = 6.96e-5 \cdot (3902 \text{ mm})^2 \cdot \frac{447474 \text{ mm}^2}{14} = 3.387e+7 \text{ mm}^4$$

App. 1-8 b-3) Step 6

$$I'_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{10.9} = 6.96e-5 \cdot (3902 \text{ mm})^2 \cdot \frac{447474 \text{ mm}^2}{10.9} = 4.35e+7 \text{ mm}^4$$

App. 1-8 b-3) Step 6

$$0.55 \cdot \sqrt{(D \cdot t_s)} = 0.55 \cdot \sqrt{(3902 \text{ mm} \cdot 42.86 \text{ mm})} = 224.9 \text{ mm}$$



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Example E4.4.7 - E4.4.8 PTB-4-2013

E4.4.7 Small End - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2021

Area at the small end of a cone-cylinder-juncture without knuckle

Type of stiffener

No stiffener

External design pressure

p_D

14.7 psi

Hydrostatic head

D_p

0 psi

Calculation pressure

p_0

14.7 psi

Calculation temperature

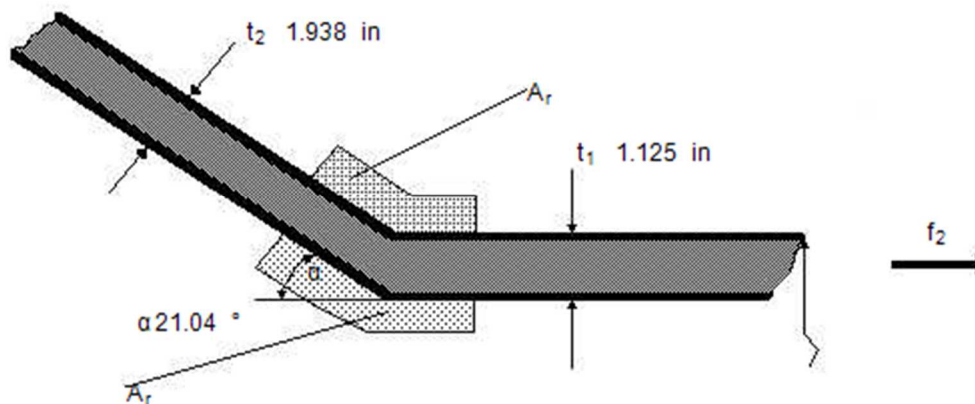
T_0

300 °F

Axial additional load as line load (positive for tension) e.g. wind load, dead weight, traffic load, etc. but no loads resulting from internal / external pressure

f_2

913 lbf/in



Cylinder

Final wall thickness

t_1

1.125 in

Wall thickness allowance

c_1

0 in

Allowance (corrosion)

c_2

0.125 in

Final thickness without allowances

t_s

1 in

Outside diameter

D_S

92.25 in

Tip radius ($=D_S/2$)

R_S

46.12 in

Required thickness without allowances (UG-28)

t_{1r}

0.6718 in

Required thickness with allowances (UG-28)

t_{1r+}

0.7968 in

Joint efficiency factor

E_1

1

Material K02700-SA-516-70-Class:-Size:

Allowable stress

S_s

20015 psi

Modulus of elasticity

E_s

2.9e+7 psi

Cone

Final wall thickness

t_2

1.938 in

Wall thickness allowance

c_1

0 in

Allowance (corrosion)

c_2

0.125 in

Final thickness without allowances

t_c

1.813 in

Semi aperture angle ($\leq 60^\circ$)

α

21.04 °

Required thickness without allowances (UG-33)

t_{2r}

0.3639 in

Required thickness with allowances (UG-33)

t_{2r+}

0.4889 in

Joint efficiency factor

E_2

1

Material K02700-SA-516-70-Class:-Size:

Allowable stress

S_c

20015 psi

Modulus of elasticity

E_c

2.9e+7 psi

Stiffening ring

Material

Actual cross section of the stiffener

A_r

in²

Allowable stress

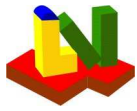
S_r

psi

Modulus of elasticity

E_r

psi



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Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Factor	k	1 ≥ 1
Effective load	Q _S	1252 lbf/in
Cross sectional area	A _{rS}	1.11 in ²
Effective area	A _{eS}	12.4 in ²
Required cross section of the stiffener	A _{req}	0 in ²
Remark		

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

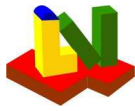
$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$Q_S = P_0 \cdot \frac{R_S}{2} + f_2 = 1.014 \text{ bar} \cdot \frac{1172 \text{ mm}}{2} + 159.9 \text{ N/mm} = 219.3 \text{ N/mm}$$

$$A_{rS} = \frac{k \cdot Q_S \cdot R_S \cdot \tan(\alpha)}{S_S \cdot E_1} = \frac{1 \cdot 219.3 \text{ N/mm} \cdot 1172 \text{ mm} \cdot 0.3846}{138 \text{ N/mm}^2 \cdot 1} = 716 \text{ mm}^2 \quad (3)$$

$$A_{eS} = 0.55 \cdot \sqrt{D_S \cdot t_s} \cdot \left[\frac{t_s - t + (t_c - t_r)}{\cos(\alpha)} \right] = \quad (4)$$

$$0.55 \cdot \sqrt{2343 \text{ mm} \cdot 25.4 \text{ mm}} \cdot \left[\frac{25.4 \text{ mm} - 17.06 \text{ mm} + (46.05 \text{ mm} - 9.242 \text{ mm})}{0.9333} \right] = 8002 \text{ mm}^2$$



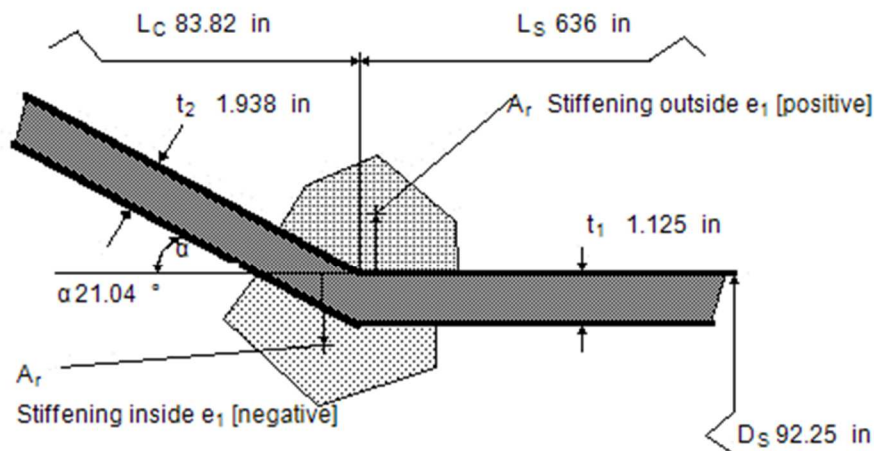
ASME BPVC VIII-1 2021
Example E4.4.7 - E4.4.8 PTB-4-2013

E4.4.7 Small End/Line-of-support - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2021

Moment of inertia at the small end of a cone-cylinder-juncture under external pressure acc. App.1-8

(Line-of-support)

External design pressure	p_D	14.7 psi
Hydrostatic head	D_p	0 psi
Calculation pressure	p_0	14.7 psi
Calculation temperature	T_0	300 °F
Axial additional load as line load (positive for tension) e.g. wind load, dead weight, traffic load, etc. but no loads resulting from internal / external pressure	f_2	913 lbf/in



Cylinder

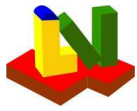
Final wall thickness	t_1	1.125 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Final thickness without allowances	t_s	1 in
Required thickness without allowances (UG-28)	t_{1r}	0.6718 in
Required thickness with allowances (UG-28)	t_{1rt}	0.7968 in
Outside diameter	D_S	92.25 in
Tip radius ($=D_S/2$)	R_S	46.12 in
Buckling length	L_S	636 in

Cone

Final wall thickness	t_2	1.938 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Final thickness without allowances	t_c	1.813 in
Required thickness without allowances (UG-33)	t_{2r}	0.3639 in
Required thickness with allowances (UG-33)	t_{2rt}	0.4889 in
Semi-apex angle ($\leq 60^\circ$)	α	21.04 °
Buckling length	L_C	83.82 in

Stiffening ring

Material	K02700-SA-516-70-Class:-Size:	
Spec. Min. Yield	S_y	2.9e+7 psi
Applicable material chart	Fig	CS-2
Radial distance between the centroid of the stiffening ring and the outer surface of the cylinder	e_1	in
Cross sectional area	A_r	0 in ²
Moment of inertia	I_r	in ⁴



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Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Equivalent length	N	362.3 in
Effective load	F _S	5677 lbf/in
Reference area	A _{TS}	394 in ²
Factor	B	997 psi
Factor (see material chart)	A	6.998e-5
Required moment of inertia	I _s	16.76 in ⁴
Required moment of inertia	I' _s	21.53 in ⁴
Length of support	0.55 · √(D · t _s)	5.283 in
Available moment of inertia	I'	in ⁴
Remark		

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\sin(\alpha) = \sin(\alpha) = \sin(21.04^\circ) = 0.359$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$R_s = R_L - L_C \cdot \sin(\alpha) = 1952 \text{ mm} - 2129 \text{ mm} \cdot 0.359 = 1172 \text{ mm}$$

$$N = \frac{R_s \cdot \tan(\alpha)}{2} + \frac{L_s}{2} + \frac{RL^2 - RS^2}{6 \cdot R_s \cdot \tan(\alpha)} =$$

$$\frac{1172 \text{ mm} \cdot 0.3846}{2} + \frac{16154 \text{ mm}}{2} + \frac{(1952 \text{ mm})^2 - (1172 \text{ mm})^2}{6 \cdot 1172 \text{ mm} \cdot 0.3846} = 9203 \text{ mm}$$

$$994.3 \text{ N/mm} = 1.014 \text{ bar} \cdot 9203 \text{ mm} + 159.9 \text{ N/mm} \cdot 0.3846$$

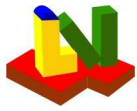
$$A_{TS} = L_s \cdot \frac{t_s}{2} + L_C \cdot \frac{t_c}{2} + A_s = 16154 \text{ mm} \cdot \frac{25.4 \text{ mm}}{2} + 2129 \text{ mm} \cdot \frac{46.05 \text{ mm}}{2} + 0 \text{ mm}^2 = 254182 \text{ mm}^2$$

$$B = \frac{3}{4} \cdot \frac{F_s \cdot D_s}{A_{TS}} = \frac{3}{4} \cdot \frac{994.3 \text{ N/mm} \cdot 2343 \text{ mm}}{254182 \text{ mm}^2} = 6.874 \text{ N/mm}^2$$

$$I_s = \frac{A \cdot DS^2 \cdot A_{TS}}{14} = \frac{6.998e-5 \cdot (2343 \text{ mm})^2 \cdot 254182 \text{ mm}^2}{14} = 6975754 \text{ mm}^4$$

$$I'_s = \frac{A \cdot DS^2 \cdot A_{TS}}{10.9} = \frac{6.998e-5 \cdot (2343 \text{ mm})^2 \cdot 254182 \text{ mm}^2}{10.9} = 8959684 \text{ mm}^4$$

$$0.55 \cdot \sqrt{(D \cdot t_s)} = 0.55 \cdot \sqrt{(D \cdot 25.4 \text{ mm})} = 134.2 \text{ mm}$$



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Example E4.4.7 - E4.4.8 PTB-4-2013

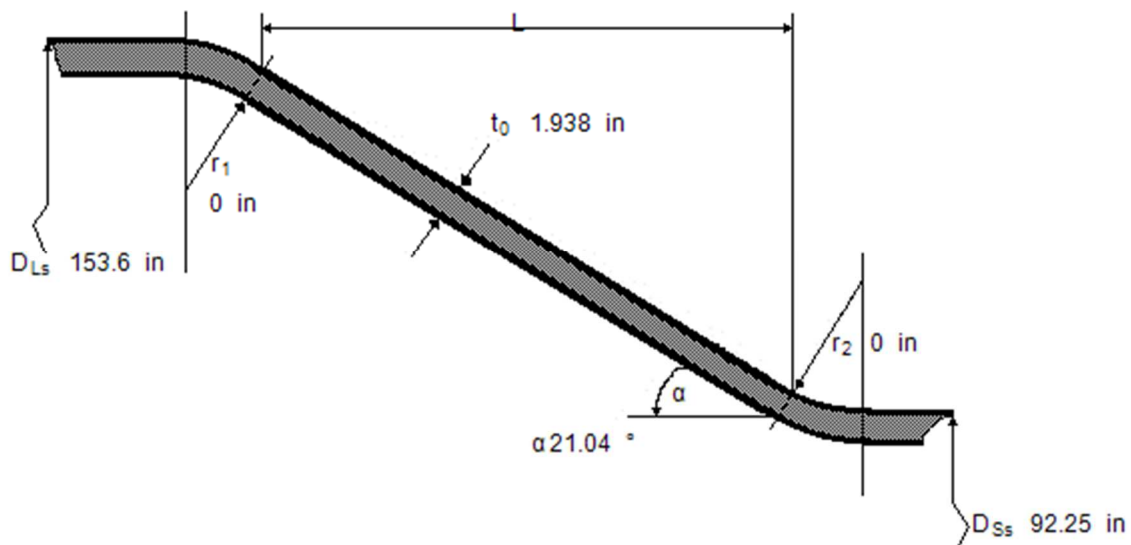
E4.4.8 Large and Small End - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2021

Conical shells under external pressure acc. UG-33(f)

External design pressure	p_D	14.7 psi
Hydrostatic head	D_p	0 psi
Calculation pressure	p_0	14.7 psi
Calculation temperature	T_0	300 °F

Material K02700-SA-516-70-Class:-Size:

Spec. Min. Yield	S_y	37710 psi
Allowable stress	S_0	20015 psi
Applicable material chart	Fig	CS-2
Modulus of elasticity	E	2.9e+7 psi

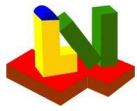


Cone wall thickness with allowances	t_0	1.938 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0.125 in
Cone wall thickness without allowances	t	1.813 in

Is a cylinder connected, which does not act as line of support?

	N	(Y/N)
Outside diameter (wide end)	D_{Ls}	153.6 in
Knuckle radius (wide end)	r_1	0 in
Outside diameter (small end)	D_{Ss}	92.25 in
Knuckle radius (small end)	r_2	0 in
Half apex angle ($\leq 60^\circ$)	α	21.04 °

Proof for cross-section area according to App. 1-8 required for cone-connection without knuckle



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Example E4.4.7 - E4.4.8 PTB-4-2013

Results

Effective thickness	$t_e = t \cdot \cos(\alpha)$	t_e	1.692 in
Axial length of the cone		L	79.79 in
Design length		L_e	63.85 in
Ratio		L_e/D_L	0.4156
Ratio		D_L/t_e	90.81
Factor according to fig. 5-UGO-28.0		A	0.004054
Factor (see material chart)		B	16850 psi
Factor	$2 \cdot \text{Min}(S_0, 9 \cdot B)$	S	31589 psi
Allowable external pressure (for t_0)		P	247.4 psi
Allowable pressure without hydrostatic head		MEP	247.4 psi
Required thickness (for P_0)		t	0.3664 in
Required thickness incl. allowances		$t+c_1+c_2$	0.4914 in

Remark

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(21.04^\circ) = 0.9333$$

$$\sin(\alpha) = \sin(\alpha) = \sin(21.04^\circ) = 0.359$$

$$\tan(\alpha) = \tan(\alpha) = \tan(21.04^\circ) = 0.3846$$

$$D_L = D_{Ls} - r_1 \cdot (1 - \cos(\alpha)) = 3902 \text{ mm} - 0 \text{ mm} \cdot (1 - 0.9333) = 3902 \text{ mm}$$

$$D_S = D_{Ss} + r_2 \cdot (1 - \cos(\alpha)) = 2343 \text{ mm} + 0 \text{ mm} \cdot (1 - 0.9333) = 2343 \text{ mm}$$

$$L = \frac{(D_L - D_S)}{2} \cdot \tan(\alpha) = \frac{(3902 \text{ mm} - 2343 \text{ mm})}{2} \cdot 0.3846 = 2027 \text{ mm}$$

$$L_1 = r_1 \cdot \sin(\alpha) = 0 \text{ mm} \cdot 0.359 = 0 \text{ mm}$$

$$L_2 = r_2 \cdot \left(\frac{D_{Ss}}{D_{Ls}} \right) \cdot \sin(\alpha) = 0 \text{ mm} \cdot 0.6005 \cdot 0.359 = 0 \text{ mm}$$

$$L_3 = \frac{L}{2} \cdot \frac{(D_L + D_S)}{D_{Ls}} = \frac{2027 \text{ mm}}{2} \cdot \frac{(3902 \text{ mm} + 2343 \text{ mm})}{3902 \text{ mm}} = 1622 \text{ mm}$$

$$L_e = L_1 + L_2 + L_3 = 0 \text{ mm} + 0 \text{ mm} + 1622 \text{ mm} = 1622 \text{ mm}$$

1) for $D_L/t_0 \geq 10$

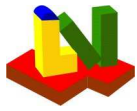
$$Pa(B) = \frac{4 \cdot B}{3 \cdot \left(\frac{D_L}{t_0} \right)} = \frac{4 \cdot 116.2 \text{ N/mm}^2}{3 \cdot 90.81} = 1.706 \text{ N/mm}^2$$

UG-33 f-a) Step 6

$$Pa(E) = \frac{2 \cdot A \cdot E}{3 \cdot \left(\frac{D_L}{t_0} \right)} = \frac{2 \cdot 0.004054 \cdot 199948 \text{ N/mm}^2}{3 \cdot 90.81} = 5.951 \text{ N/mm}^2$$

UG-33 f-a) Step 7

2) for $D_L/t_0 < 10$



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Example E4.4.7 - E4.4.8 PTB-4-2013

$$P_{a1} = \left[\frac{2.167}{\frac{D_L}{t_0}} - 0.0833 \right] \cdot B = \left[\frac{2.167}{90.81} - 0.0833 \right] \cdot 116.2 \text{ N/mm}^2 = -6.905 \text{ N/mm}^2$$

UG-33 f-b) Step 2

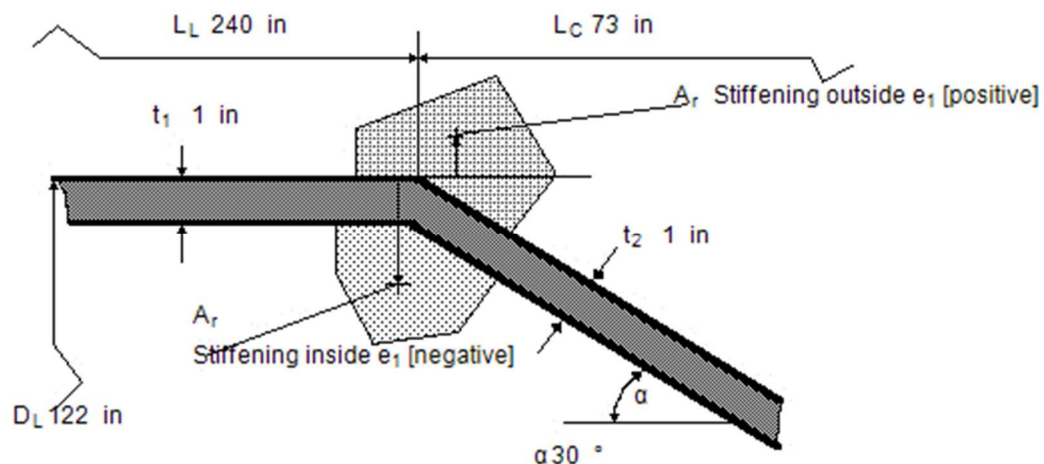
$$P_{a2} = \frac{2 \cdot S}{\frac{D_L}{t_0}} \cdot \left[1 - \frac{2 \cdot S}{\frac{D_L}{t_0}} \right] = \frac{2 \cdot 217.8 \text{ N/mm}^2}{90.81} \cdot \left[1 - \frac{2 \cdot 217.8 \text{ N/mm}^2}{90.81} \right] = 4.744 \text{ N/mm}^2$$

UG-33 f-b) Step 3

E4.4.8 Large End/Line-of-support - Formed heads pressure under external pressure - ASME BPVC VIII-1 UG-33 & Appendix-1: 2021

Moment of inertia at the wide end of a cone-cylinder-juncture under external pressure acc. App. 1-8 (Line-of-support)

External design pressure	p_D	14.7 psi
Hydrostatic head	D_p	0 psi
Calculation pressure	p_0	14.7 psi
Calculation temperature	T_0	300 °F
Axial additional load as line load (positive for tension) e.g. wind load, dead weight, traffic load, etc. but no loads resulting from internal / external pressure	f_1	145 lbf/in

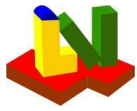


Cylinder

Design wall thickness	t_1	1 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0 in
Final thickness without allowances	t_s	1 in
Required thickness without allowances (UG-28)	t_{1r}	0.5205 in
Required thickness with allowances (UG-28)	t_{1r+}	0.5205 in
Outside diameter	D_L	122 in
Tip radius	R_L	61 in
Buckling length	L_L	240 in

Cone

Design wall thickness	t_2	1 in
Wall thickness allowance	c_1	0 in
Allowance (corrosion)	c_2	0 in
Final thickness without allowances	t_c	1 in



ASME BPVC VIII-1 2021

Example E4.4.7 - E4.4.8 PTB-4-2013

Required thickness without allowances (UG-33)	t_{2r}	0.3358 in
Required thickness with allowances (UG-33)	t_{2r+}	0.3358 in
Half apex angle ($\leq 60^\circ$)	α	30 °
Buckling length	L_C	73 in

Stiffening ring

Material	K02700-SA-516-70-Class:-Size:	
Spec. Min. Yield	S_y	2.9e+7 psi
Applicable material chart	Fig	CS-2
Radial distance between the centroid of the stiffening ring and the outer surface of the cylinder	e_1	0 in
Cross sectional area	A_r	0 in ²
Moment of inertia	I_r	0 in ⁴

Results

Equivalent length	M	134.7 in
Effective load	F_L	2064 lbf/in
Reference area	A_{TL}	156.5 in ²
Factor	B	1207 psi
Factor (see material chart)	A	8.447e-5
Required moment of inertia	I_s	14.06 in ⁴
Required moment of inertia	I'_s	18.05 in ⁴
Length of support	$0.55 \cdot \sqrt{(D \cdot t_s)}$	6.075 in
Available moment of inertia	I'	18.15 in ⁴

Remark **Stiffening required**

Equations

$$\cos(\alpha) = \cos(\alpha) = \cos(30^\circ) = 0.866$$

$$\sin(\alpha) = \sin(\alpha) = \sin(30^\circ) = 0.5$$

$$\tan(\alpha) = \tan(\alpha) = \tan(30^\circ) = 0.5774$$

$$R_s = R_L - L_C \cdot \sin(\alpha) = 1549 \text{ mm} - 1854 \text{ mm} \cdot 0.5 = 445 \text{ mm}$$

$$M = \frac{-R_L \cdot \tan(\alpha)}{2} + \frac{L_L}{2} + \frac{RL^2 - RS^2}{3 \cdot R_L \cdot \tan(\alpha)} = \text{App. 1-8 b-3) Step 1}$$

$$\frac{-1549 \text{ mm} \cdot 0.5774}{2} + \frac{6096 \text{ mm}}{2} + \frac{(1549 \text{ mm})^2 - (445 \text{ mm})^2}{3 \cdot 1549 \text{ mm} \cdot 0.5774} = 3421 \text{ mm}$$

$$F_L = P_0 \cdot M + f_1 \cdot \tan(\alpha) = \text{App. 1-8 b-3) Step 1}$$

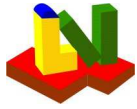
$$1.014 \text{ bar} \cdot 3421 \text{ mm} + 25.39 \text{ N/mm} \cdot 0.5774 = 361.4 \text{ N/mm}$$

$$A_{TL} = L_L \cdot \frac{t_s}{2} + L_C \cdot \frac{t_c}{2} + A_s = \text{App. 1-8 a)}$$

$$6096 \text{ mm} \cdot \frac{25.4 \text{ mm}}{2} + 1854 \text{ mm} \cdot \frac{25.4 \text{ mm}}{2} + 0 \text{ mm}^2 = 100968 \text{ mm}^2$$

$$B = \frac{3}{4} \cdot \frac{F_L \cdot D_L}{A_{TL}} = \frac{3}{4} \cdot \frac{361.4 \text{ N/mm} \cdot 3099 \text{ mm}}{100968 \text{ mm}^2} = 8.32 \text{ N/mm}^2 \quad \text{App. 1-8 b-3) Step 1}$$

$$I_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{14} = 8.447\text{e-5} \cdot (3099 \text{ mm})^2 \cdot \frac{100968 \text{ mm}^2}{14} = 5850143 \text{ mm}^4 \quad \text{App. 1-8 b-3) Step 6}$$



ASME BPVC VIII-1 2021
Example E4.4.7 - E4.4.8 PTB-4-2013

App. 1-8 b-3) Step 6

$$I'_s = A \cdot D_L^2 \cdot \frac{A_{TL}}{10.9} = 8.447 \text{e-}5 \cdot (3099 \text{ mm})^2 \cdot \frac{100968 \text{ mm}^2}{10.9} = 7513945 \text{ mm}^4$$

$$0.55 \cdot \sqrt{(D \cdot t_s)} = 0.55 \cdot \sqrt{(3099 \text{ mm} \cdot 25.4 \text{ mm})} = 154.3 \text{ mm}$$